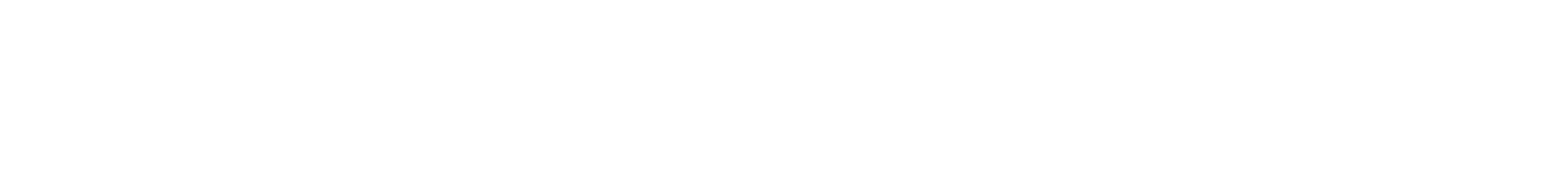
# **BACHELOR IN INFORMATION TECHNOLOGY**



# **ASSIGNMENT**

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1. Define contradiction and tautology. Show that the compound proposition [p^(p->q)]->q is tautology.

* A compound proposition is said to be contradiction if its truth value is always false. For eg:

|  |  |  |
| --- | --- | --- |
| P | ~P | P^~P |
| T | F | F |
| F | T | F |

* A compound proposition is said to be tautology if its truth value is always true . For eg:

|  |  |  |
| --- | --- | --- |
| P | ~P | Pv~P |
| T | F | T |
| F | T | T |

* Solution:

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| P | q | p->q | P^(p->q) | [p^(p->q)]->q |
| T | T | T | T | T |
| T | F | F | F | T |
| F | T | T | F | T |
| F | F | T | F | T |

Here, the above table shows that compound proposition [p^(p->q)]->q is tautology.

1. Without expanding show that

1 1 1

a b c = (a-b)(b-c)(c-a) bc ca ab

Solution: Given,

Taking L.H.S

1 1 1 a b c

bc ca ab

First step : R1->R1-R2

1-1 1 1 a-b b c

bc-ca ca ab

taking (a-b) common in first row R1 second step: R2->R2-R1

= 0 1-1 1

(a-b) 1 b-c c

-c ca-ab ab

Taking (b-c) common in second row R2

= 0 0 1 (a-b)(b-c) 1 1 c

-c -a ab

Then,

Here = 1 1 1

-c -a

= 1x-a-(-c) x1

= (c-a)

Hence, we have proved that (a-b)(b-c)(c-a)

L.H.S=R.H.S proved

1. Define homogeneous recurrence relation. Solve the recurrence relation. an=6an-1+8an-2 for n\_>2,a0=4,a1=10

* + - A homogeneous recurrence relation is said to be if the order of k of the form can be found as an=c1an-1+c2an-2+….+ckan-k

* + - Solution:

Given recurrence relation is an=6an-1+8an-2……….(i) This is the recurrence relation of second order. Its character equation is ; Or, r2=6r1-8r0

Or, r2-6r+8=0

Or, r(r-4)-2(r-4)=0

Or, (r-4)(r-2)=0

Hence, r1=2,r2=4 The solution of eqn(i) is , an= α1r1n+α2r2n

an= α12n+α24n………………….(ii)

Put n=0 in eqn(ii), we get a0=α120+α240 Given a0=4, then

Or, 4=α1+ α2

Or, α2=4-α1 again, put n=1

Or, a1=α121+α241 Given a1=10

Or, 10= α12+(4-α1)4 Or, 5=α1+8-2α1

Or, α1=3, α2=1

Here, the equation is found to be an=3x2n+1x4n

3. Define the term tree, minimum spanning tree, simple, multiple and pseudo graph. Write prim’s and kruskal’s algorithm to construct minimum spanning tree. Explain the process of generating spanning tree using kruskal’s algorithm? Assume example of your own.

* Tree: A connected undirected graph with no simple circuit is called tree .for a tree a graph must be simple graph.

* Minimum spanning tree: A spanning tree of n connected graph in which the sum of weight of it’s edge in minimal is called minimum spanning tree.
* Simple graph:
* Multiple graph:  Pseudo graph:

* Prim’s algorithm:

Procedure: G:weighted connected undirected graph with n vertices.

T:= a minimum weight edge.

For P:= 1 to n-2. Begin e:= an edge of minimum weight incident to a vertex inT and not forming a simple circuit in T if added to T.

T:= T with e added.

End{ T is a minimum spanning tree of G.}

Kruskal’s algorithm: Procedure:

Kruskal(G: a connected undirected weighted graph with n vertices.) T: = empty graph.

For : i: 1 to n-1.

Begin e:= any edge in G with smallest weight and forming a simple circuit if added to T. T:= tree with e added.

End{T is minimum spanning tree of G.}

a 5 b 4 c



2 3 5 6 3 f 7 e 1 d

6 8 3 4 4 g

4 h 2 i

Solution:

First of all we list edges in ascending order.

(e,d)=1

(h,i)=2

(a,f)=2

(b,f)=3

(e,h)=3

(c,d)=3

(b,c)=4

(d,i)=4

(d,h)=4

(g,h)=4

(b,e)=5

(a,b)=5

(f,g)=6

(b,d)=6

(e,f)=7

(f,h)=8

Step1 : take an edge with minimum weight

e 1 d

step 2: adding (h,i) and (a,f) having weight 2 on T.

e 1 d

h 2 i a 2 f

step 3 : adding (b,f),(e,h),(c,d) having weight 3 on T.

e 1 d 3 c b

3 3

h 2 i a 2 f

step 4: adding (b,c),(d,i),(d,h),(g,h) having weight 4 on T.

e 1 d 3 c

3

4

h 2 i

4

g

a 2

f

3

b

here in step 4 the circuit is formed so they are excluded (d,h),(d,i) step 5 : adding (b,e),(a,b) having weight 5 on T. here (a,b),(b,e) is excluded because it makes circuit

(f,g),(b,d),(e,f),(f,h) are also excluded

Therefore, minimum spanning tree is found to be 22 having weighted.